



P(A)	
a=0	0.5
a=1	0.5

P(B A)		
a=0	b=0	0.5
a=0	b=1	0.5
a=1	b=0	0.2
a=1	b=1	0.8

P(C A, B)			
a=0	b=0	c=0	0.8
a=0	b=0	c=1	0.2
a=0	b=1	c=0	0.6
a=0	b=1	c=1	0.4
a=1	b=0	c=0	0.2
a=1	b=0	c=1	0.8
a=1	b=1	c=0	0.1
a=1	b=1	c=1	0.9

P(D C)		
c=0	d=0	0.4
c=0	d=1	0.6
c=1	d=0	0.2
c=1	d=1	0.8

Answer the question based on the given Bayes Net. All variables have domains of $\{0, 1\}$

- (1) Before eliminating any variables or including any evidence, how many entries does the factor $f(C,A,B)$ have?
- (2) Now to answer the query $P(B|d=1)$, you pick C as the first variable to be eliminated. How many entries does the factor have if we eliminate C?
- (3) Compute the result of joining $P(B|A)$ and $P(C|A, B)$? And the result if we further marginalize over B?

(1) The factor is $P(C|A, B)$. Because none of the variable elimination is done, we have $2^3 = 8$ entries.

(2) $f(A, B, d) = \sum_{c \in \{-0, 1\}} p(B|A)p(c|A, B)p(d|c)$. So the factor as $2^2=4$ entries.

(3) By joining $P(B|A)$ and $P(C|A, B)$, we have $P(C, B|A)$. And its corresponding distribution table is as follows:

P(C, B A)			
a=0	b=0	c=0	0.4
a=0	b=0	c=1	0.1
a=0	b=1	c=0	0.3
a=0	b=1	c=1	0.2
a=1	b=0	c=0	0.04
a=1	b=0	c=1	0.16
a=1	b=1	c=0	0.08
a=1	b=1	c=1	0.72

Each entry is computed by: $p(c, b|a)$
 $= p(b|a)p(c|a, b)$.

(continuing) And we further marginalize $P(C, B|A)$ over B , and we can obtain the distribution $p(C|A)$:

P(C A)		
a=0	c=0	0.7
a=0	c=1	0.3
a=1	c=0	0.12
a=1	c=1	0.88

Each entry is computed by: $p(c|a) = \sum_b p(c, b|a)$.